

# Chaos in micro-mechanics: towards MEMS-based secured communications

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Martial Defoort

with Libor Rufer, Yosra Azzouz, Nathan Le Gousse,  
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Univ. Grenoble Alpes, CNRS, Grenoble INP, TIMA



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## Pluto's moon Nix



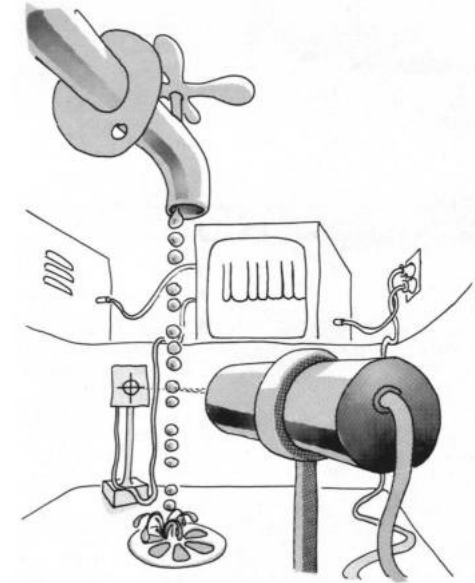
nasa.gov

## The Swinging Sticks



GeelongShop.com

## Dripping faucet



P. Martien *et al*, Physics Letters (1985)

### Chaotic regime:

- Complex interactions within at least 3D in phase space
- Non-periodic yet *deterministic*
- Exponentially sensitive to initial conditions

## Random numbers

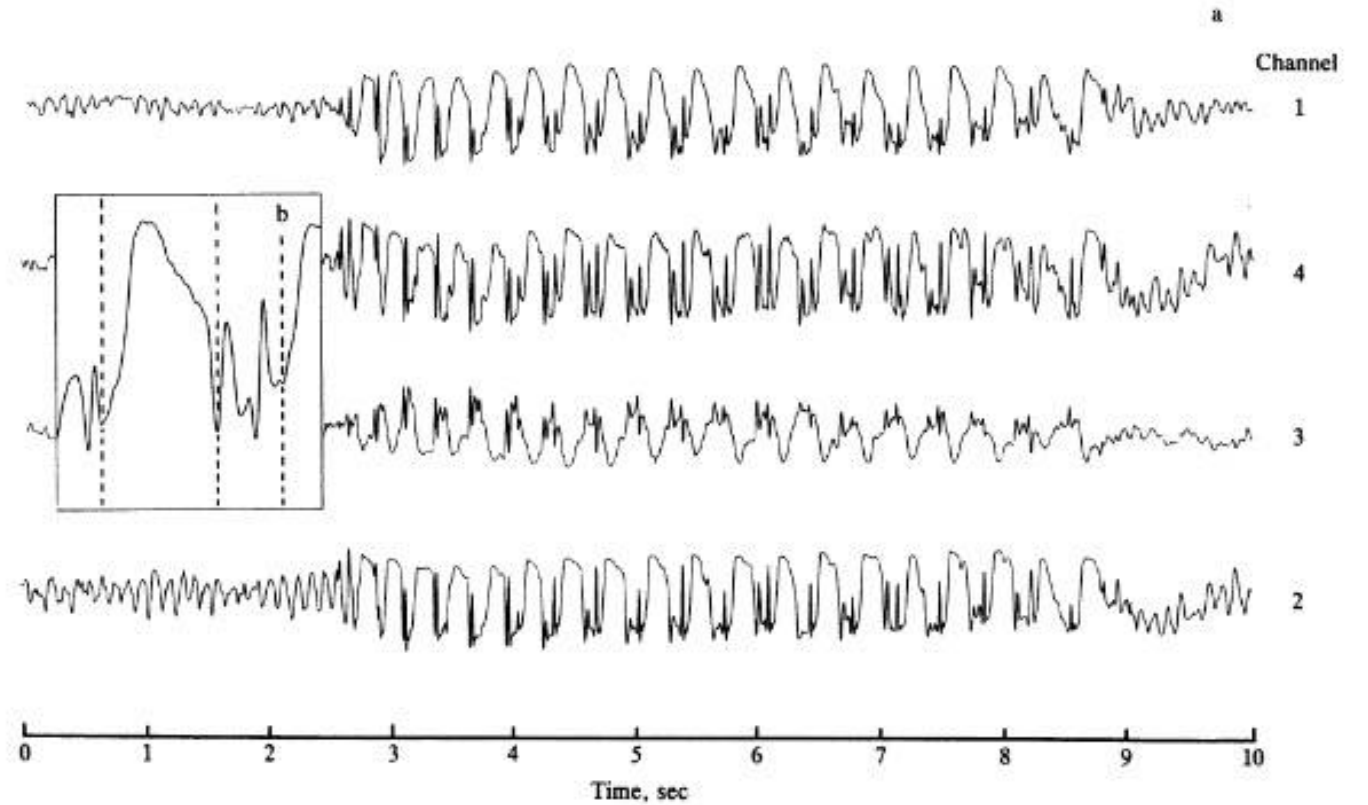


Cloudflare

## Weather



## Epileptic seizure



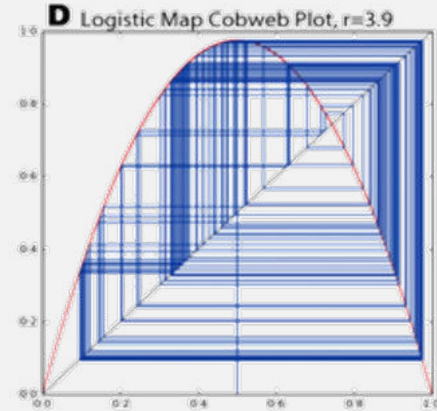
A. Babloyantz *et al*, PNAS (1986)

## Mathematically

The logistic map

$$x_{n+1} = r x_n (1 - x_n)$$

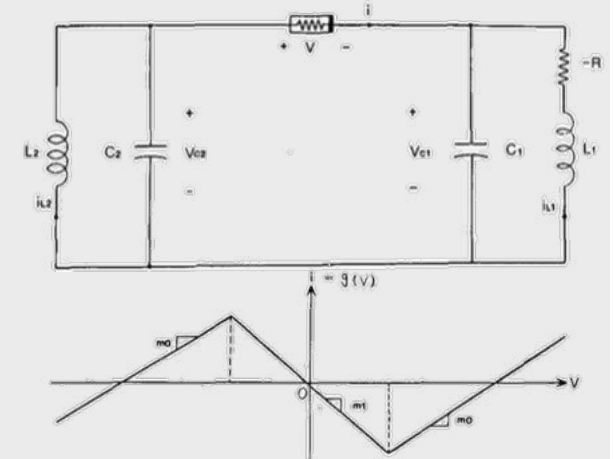
with  $3.57 \leq r \leq 4$



Boeing, PhD (2017)

## Electronically

Chua circuits

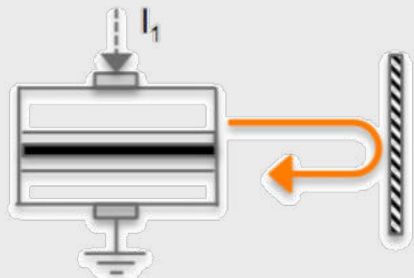


Nonlinear resistance

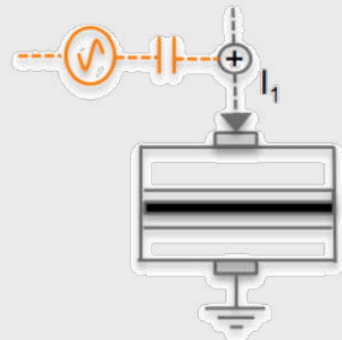
Matsumoto, IEEE TCS (1986)

## Optically

Optical feedback



Current modulation



Sciamanna, Nature Photonics (2015)

## Mechanically

Buckled structures

State of the art in MEMS: capacitive control



Miandoab *et al*, CNSNS (2015)  
Barcelò *et al*, MEMS (2018)

Active buckling :  
10-100 V continuous

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Martial Defoort

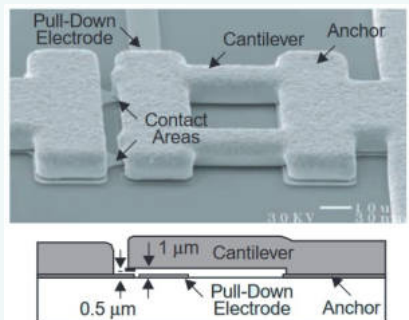
with Libor Rufer, Yosra Azzouz, Nathan Le Gousse,  
Laurent Fesquet, Skandar Basrour

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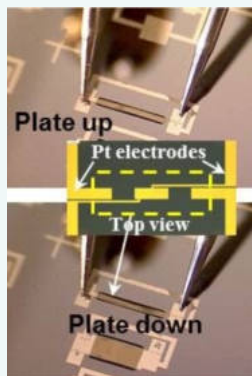
## Non-resonant

### RF switches



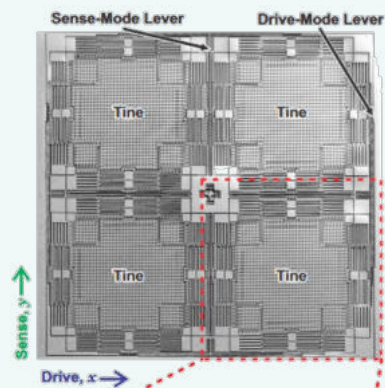
Analog Devices, (2001)

### Energy Harvesters



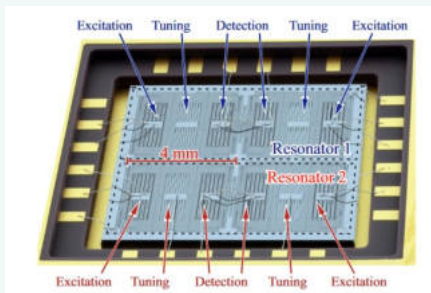
E. Trioux,  
IEEE Sensors (2014)

### Gyroscopes



I.P. Prikhodko *et al*,  
Solid State Sensors (2011)

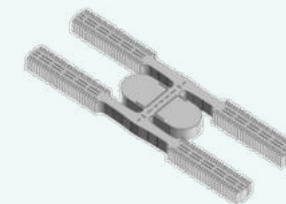
### Accelerometers



S. A. Zotov,  
IEEE Sensors (2015)

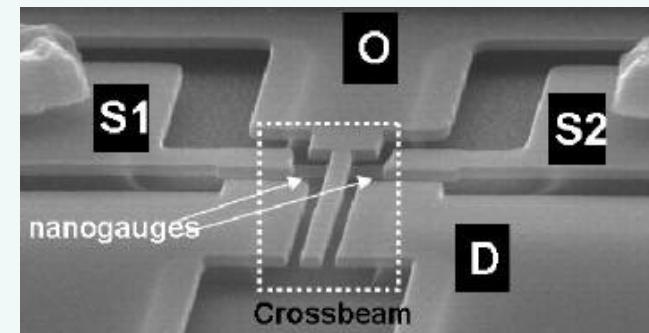
## Resonant

### Clocks

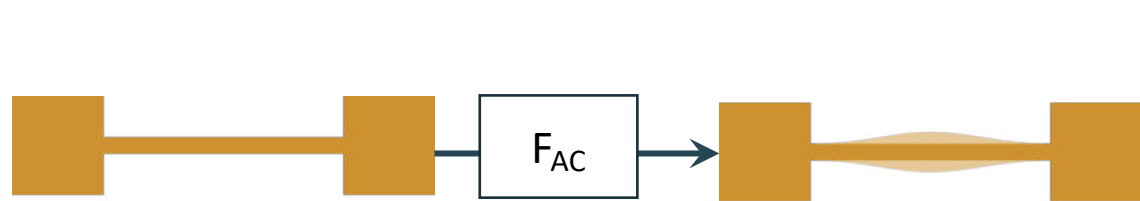


SiTime, (2017)

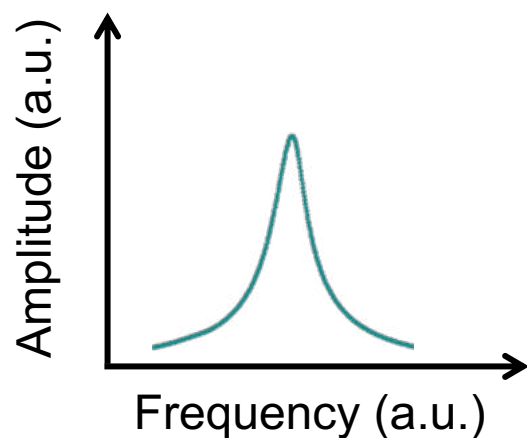
### Gas sensors



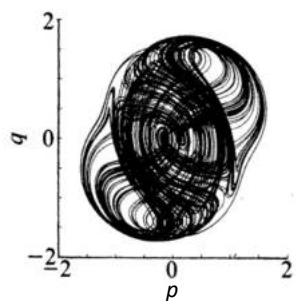
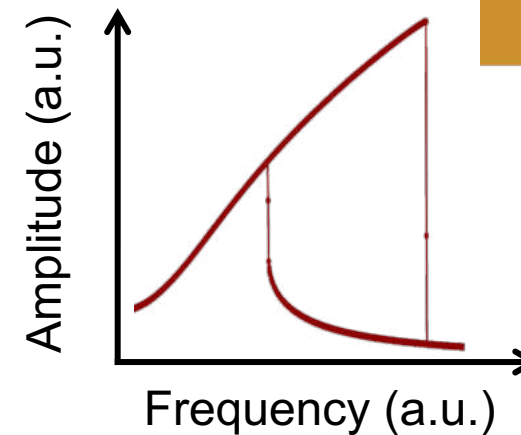
J. Arcamone, IEDM (2011)



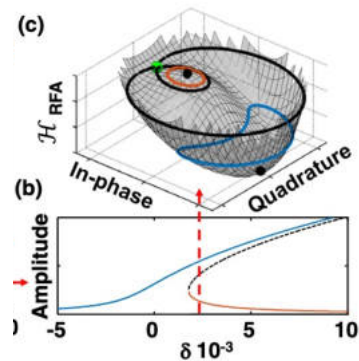
Linear regime



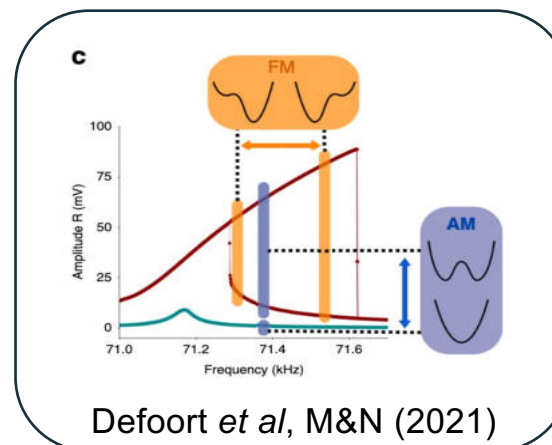
Duffing regime



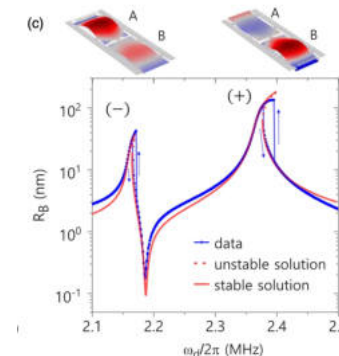
Miles, PNAS (1984)



Houri *et al*, PRL (2020)



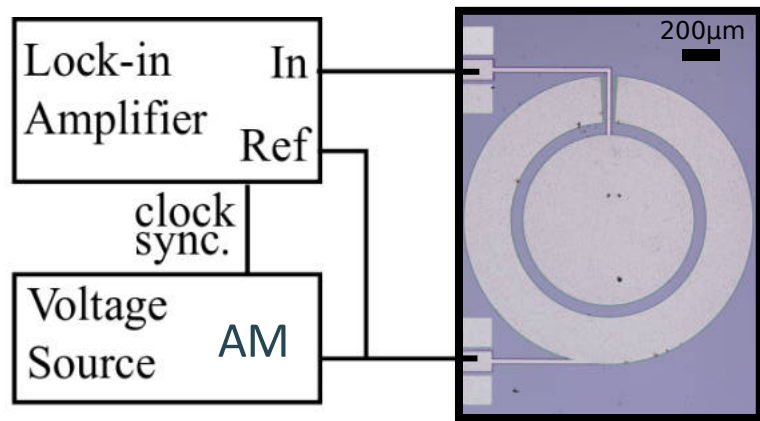
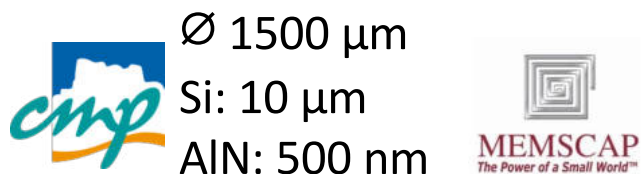
Defoort *et al*, M&N (2021)



Madiot *et al*, PRA (2021)



Setup



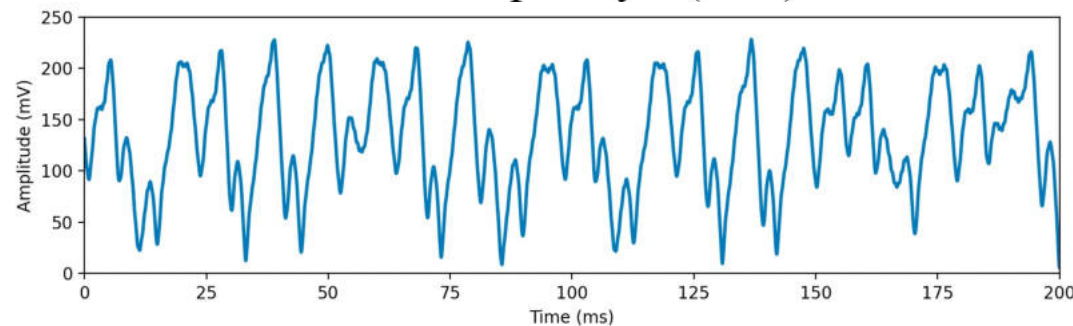
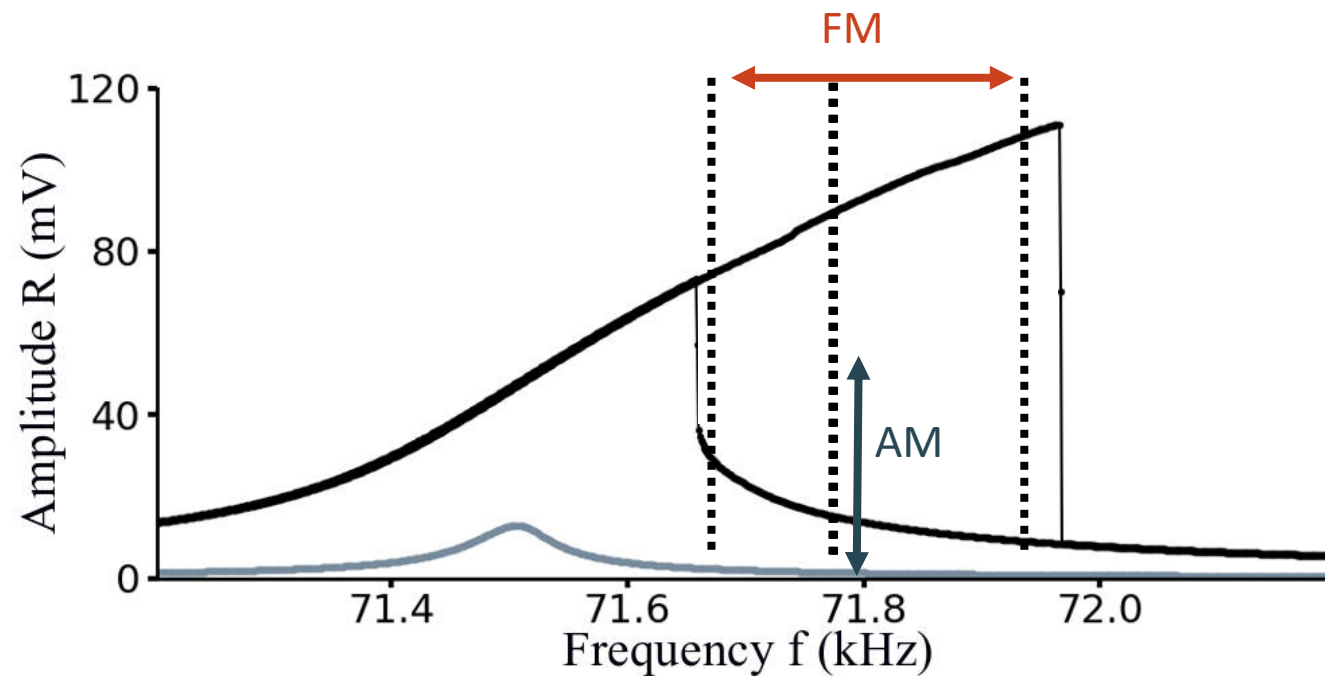
$$\ddot{x} + \Delta\omega \dot{x} + \omega_0^2 x + \alpha x^3 = \frac{F}{m}$$

FM:  $F \rightarrow F_0 \cos(\omega t + \sin(\delta\omega t))$

AM:  $F \rightarrow F_0 \cos(\omega t) \frac{1 + \cos(\delta\omega t)}{2}$

$f_0 = 71.5 \text{ kHz}$

$Q = 1100 @ 1\text{mbar}$

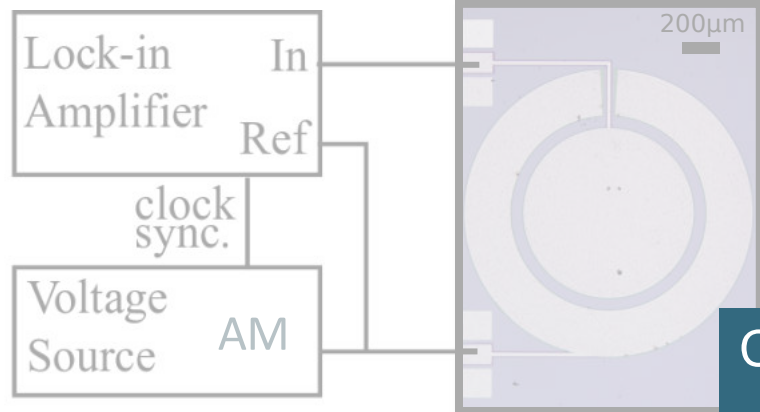


Fast modulation  $\longrightarrow$  system never at equilibrium  $\longrightarrow$  new physics

Setup

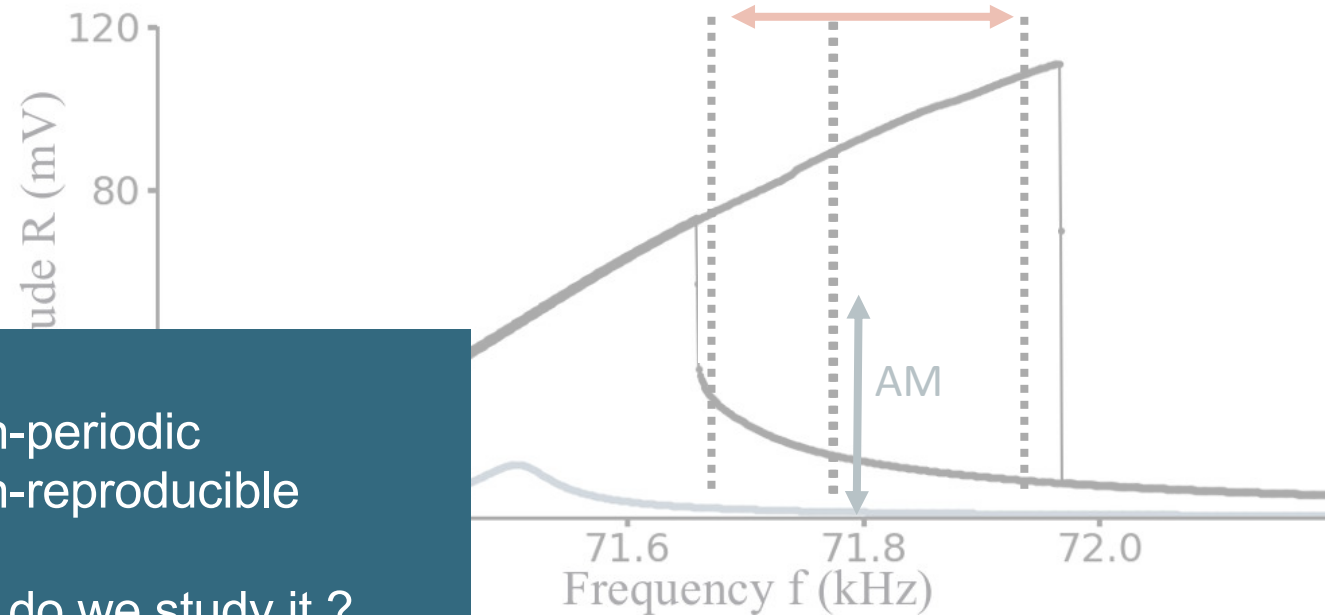


Ø 1500 µm  
Si: 10 µm  
AlN: 500 nm



$f_0 = 71.5$  kHz

$Q = 1100$  @ 1mbar



Chaos:

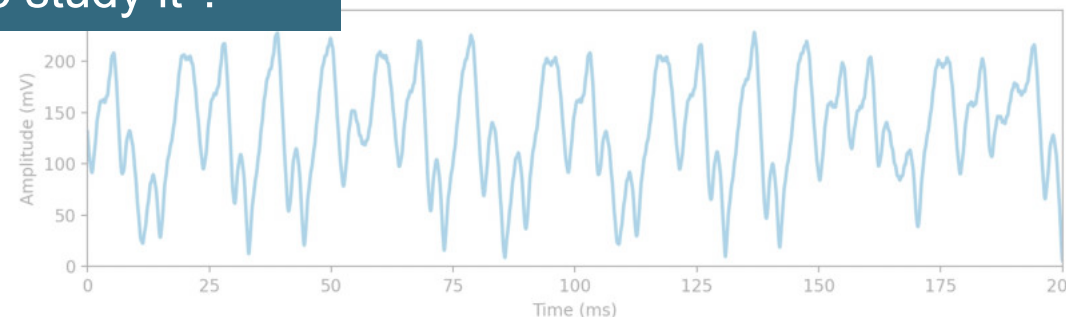
- non-periodic
- non-reproducible

How do we study it ?

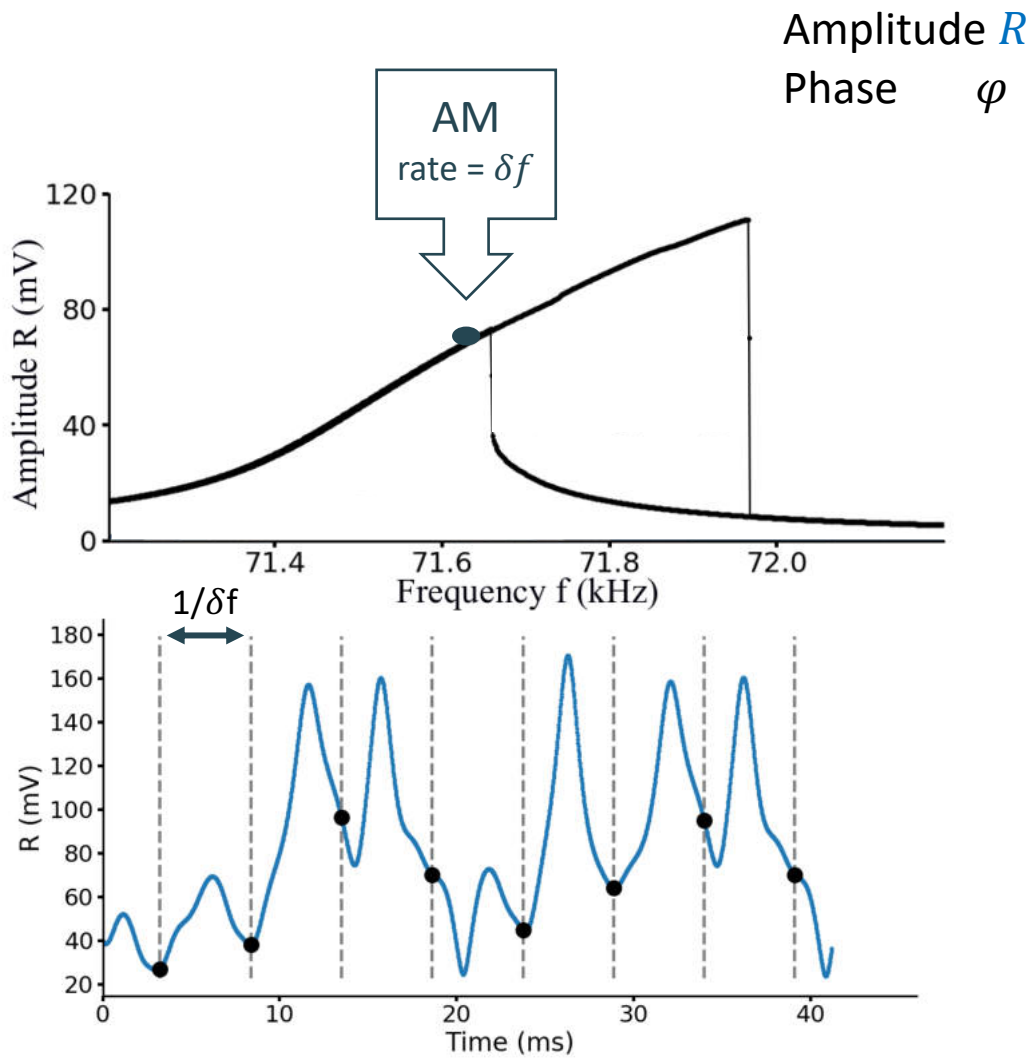
$$\ddot{x} + \Delta\omega \dot{x} + \omega_0^2 x + \alpha x^3 = \frac{F}{m} \cos(\omega t)$$

FM:  $F \rightarrow F_0 \cos(\omega t + \sin(\delta\omega t))$

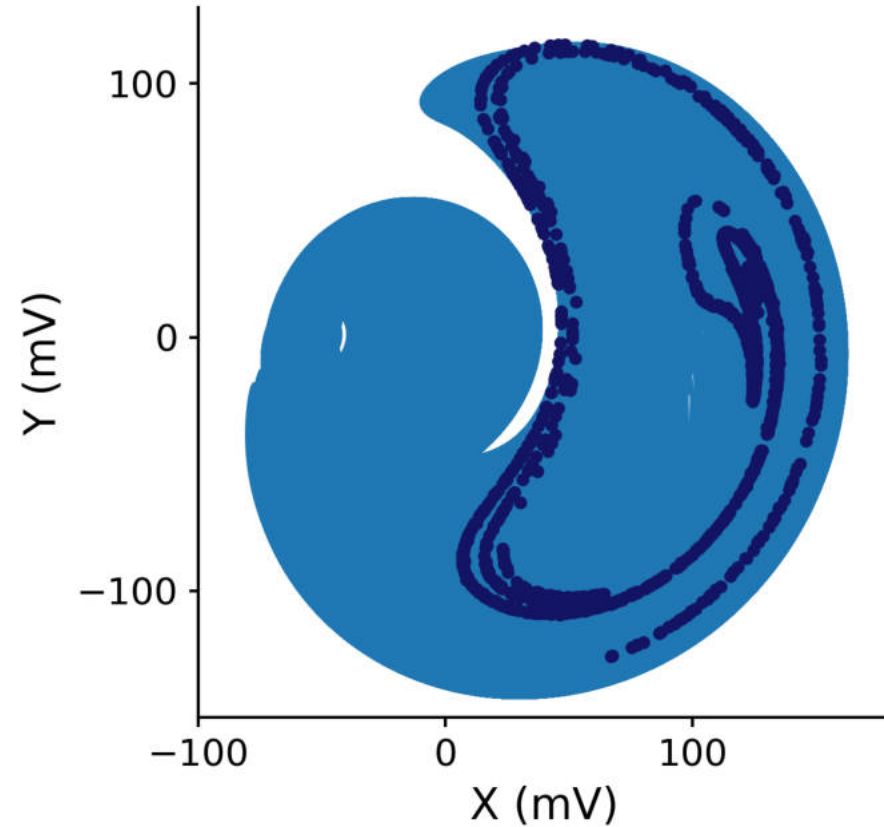
AM:  $F \rightarrow F_0 \cos(\omega t) \frac{1 + \cos(\delta\omega t)}{2}$



Fast modulation → system never at equilibrium → new physics



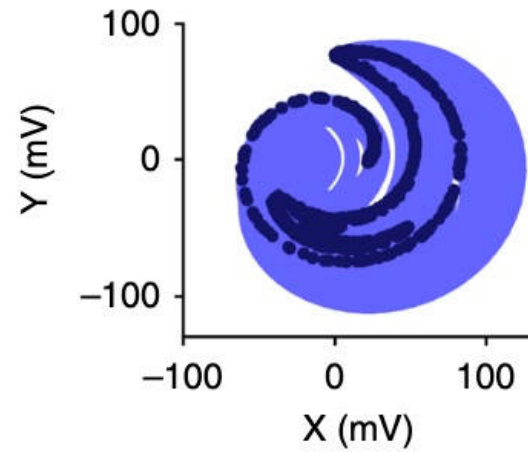
$$X = R \cos \varphi$$
$$Y = R \sin \varphi$$



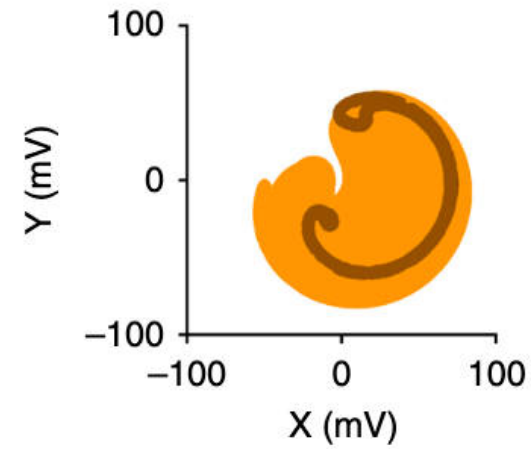
Poincaré sections: order within chaos

Experimental

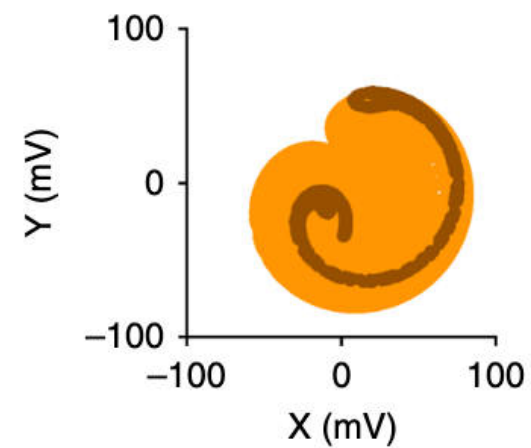
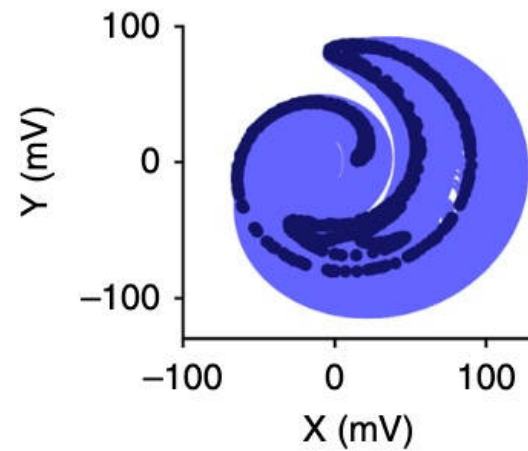
Amplitude Modulation

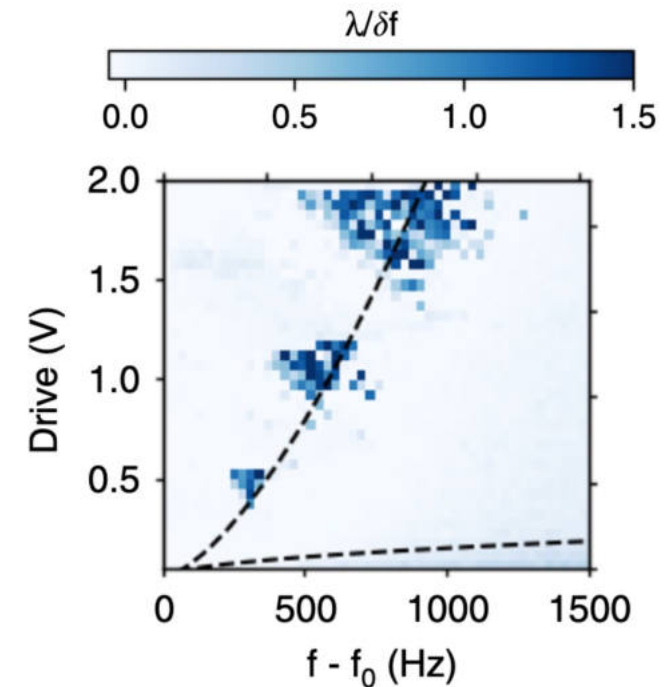
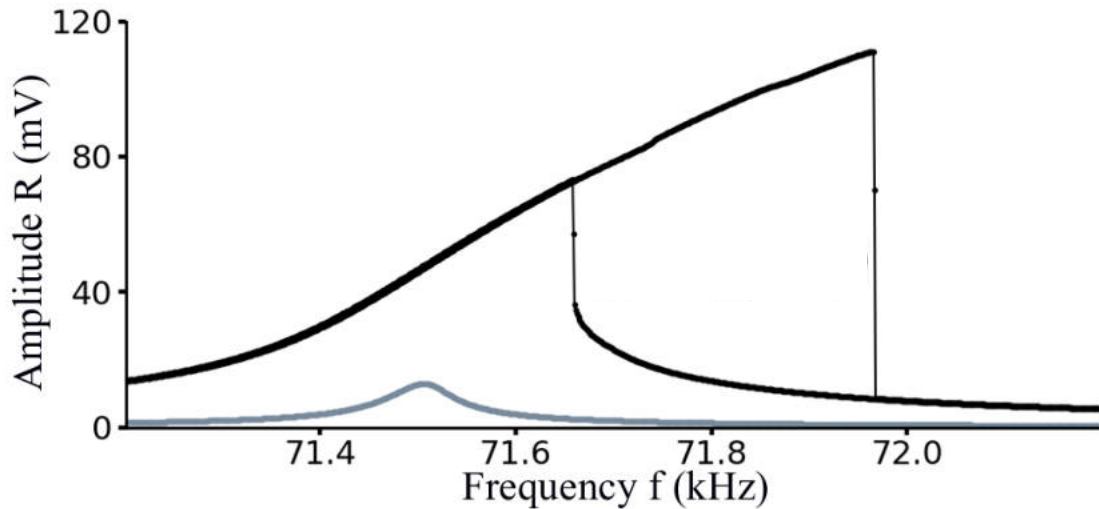
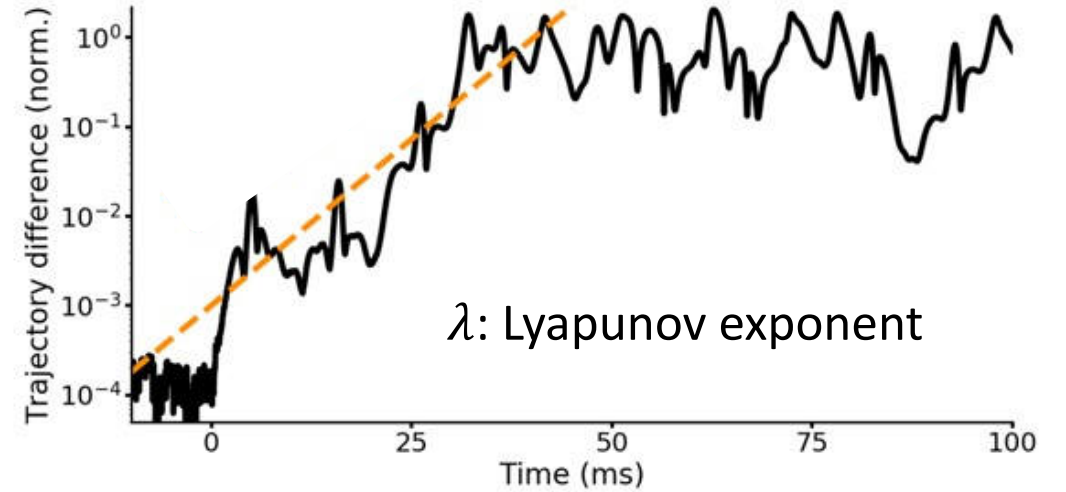
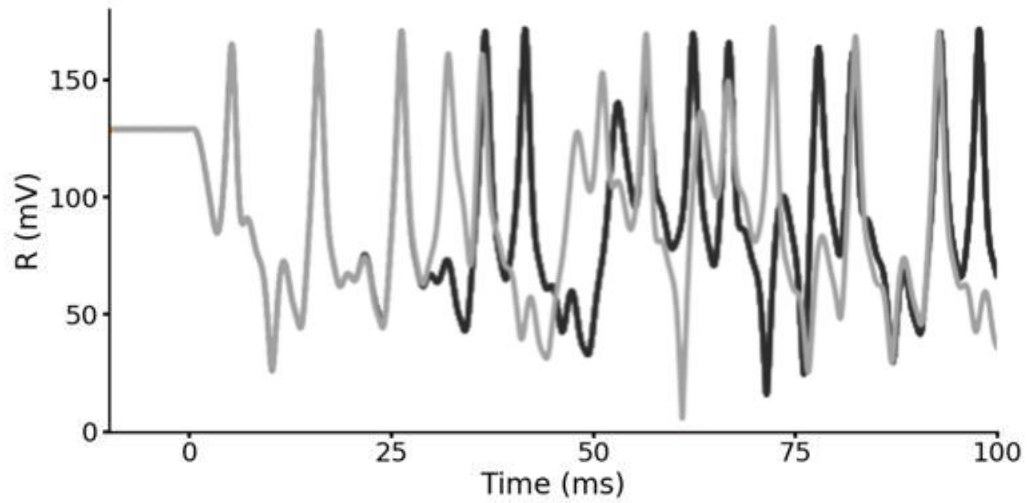


Frequency Modulation



Numerical



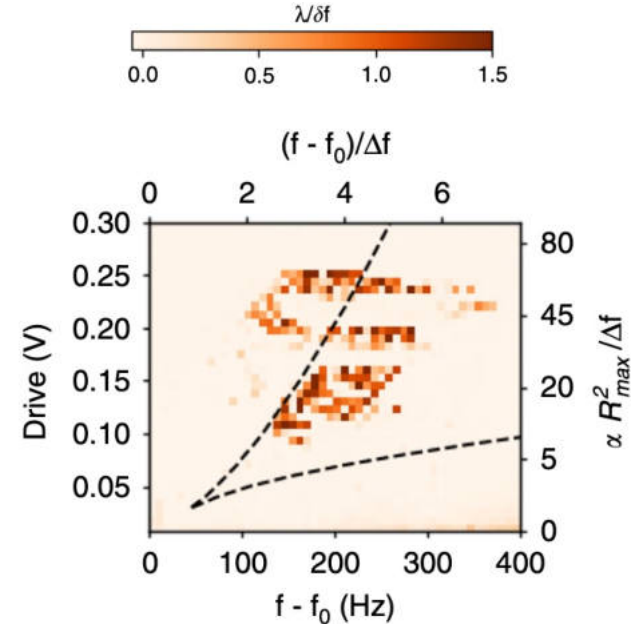
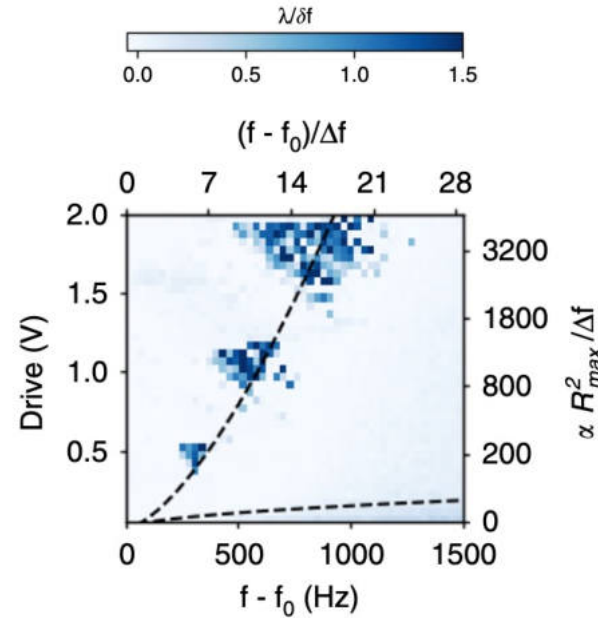


AM: 
$$F \rightarrow F_0 \cos(\omega t) \frac{1 + \cos(\delta\omega t)}{2}$$

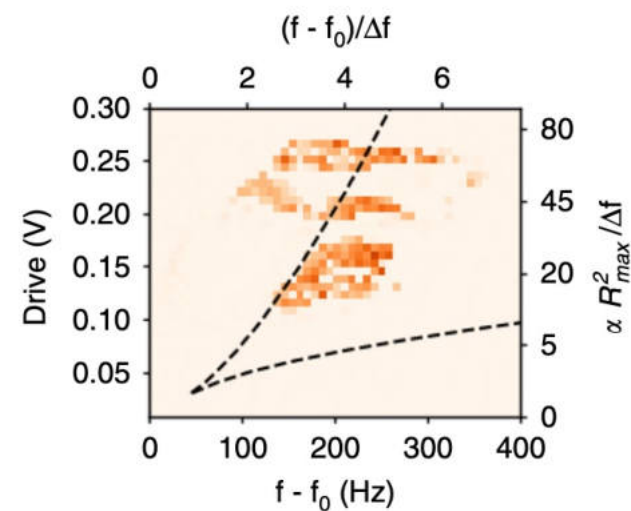
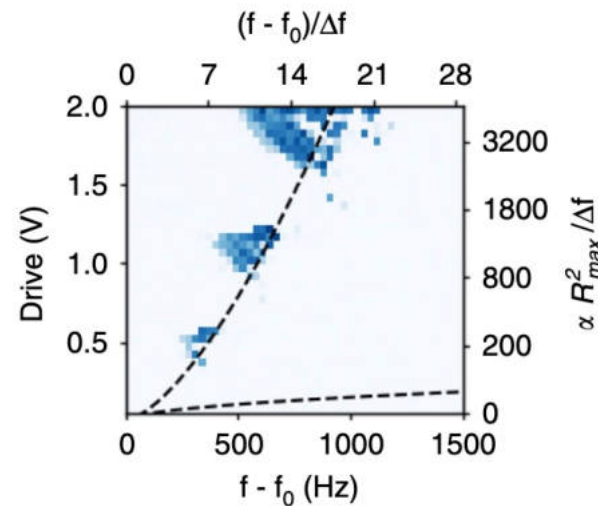
## Amplitude Modulation

## Frequency Modulation

Experimental



Numerical



# Chaos in micro-mechanics: towards MEMS-based secured communications

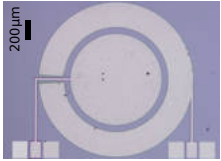
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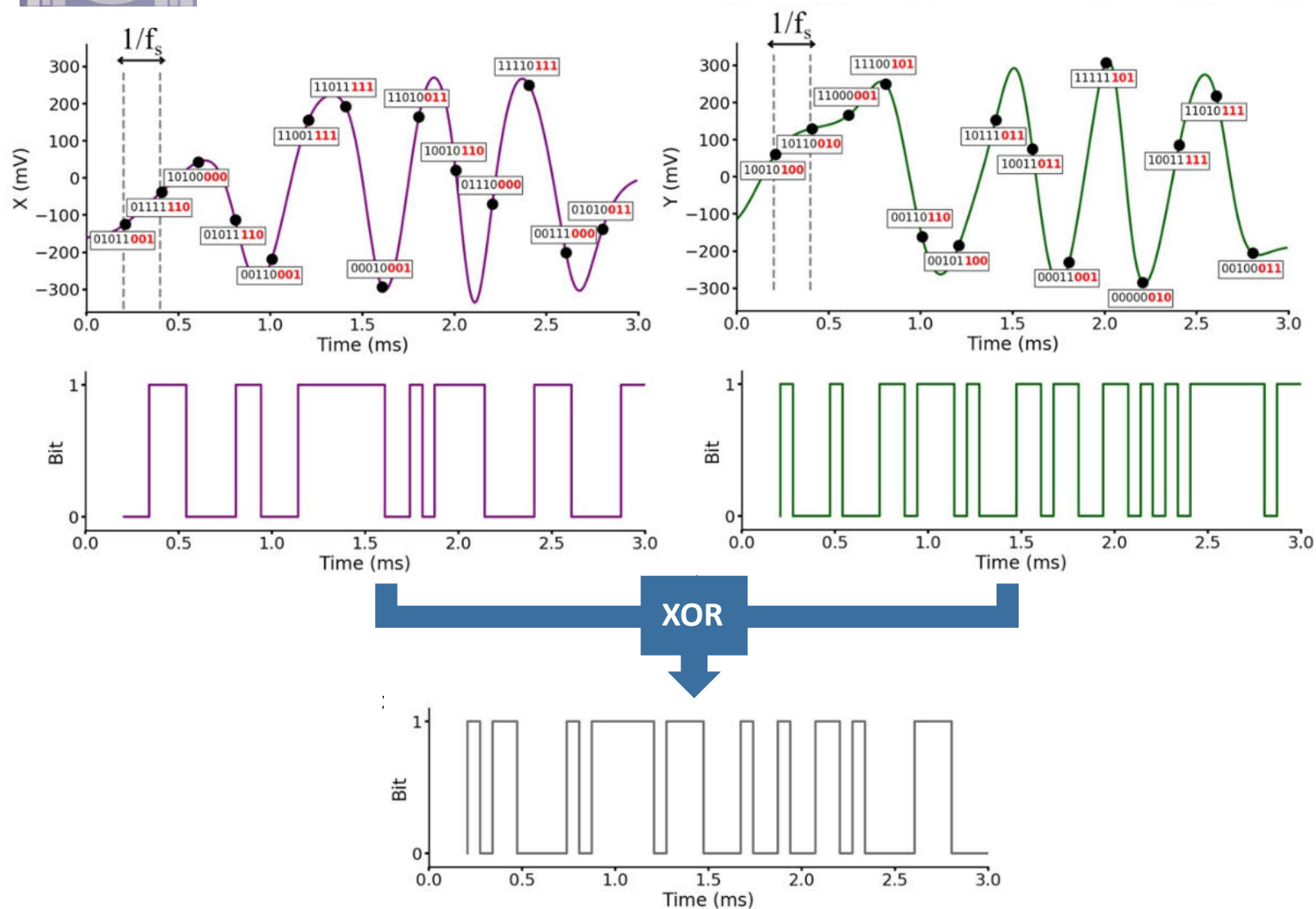
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## 3 Last Significant Bits of an 8-bit ADC

## NIST 800-22 test on 75 Mb with a rate of 15 kb/s



Test	p-Value	Proportion	Result
Frequency	0.044425	75/75	Pass
Block Frequency	0.754127	73/75	Pass
Cumulative Sums	0.622341	150/150	Pass
Runs	0.099089	75/75	Pass
Longest Run	0.491599	75/75	Pass
Rank	0.666838	75/75	Pass
FFT	0.069925	74/75	Pass
NOT Matching	0.419859	11008/11100	Pass
OT Matching	0.009343	74/75	Pass
Universal	0.548605	74/75	Pass
Approx. Entropy	0.015444	74/75	Pass
Random Excursion	0.433207	371/376	Pass
Random Exc. Var.	0.393372	839/846	Pass
Serial	0.650162	150/150	Pass
Linear Excursion	0.256632	75/75	Pass

Defoort *et al*, *Microsyst. Nanoeng.* (2021)

Defoort *et al*, *patent* (2022)



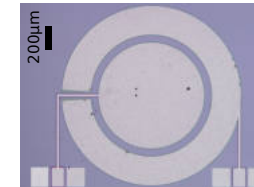


## Moths jam bats to survive

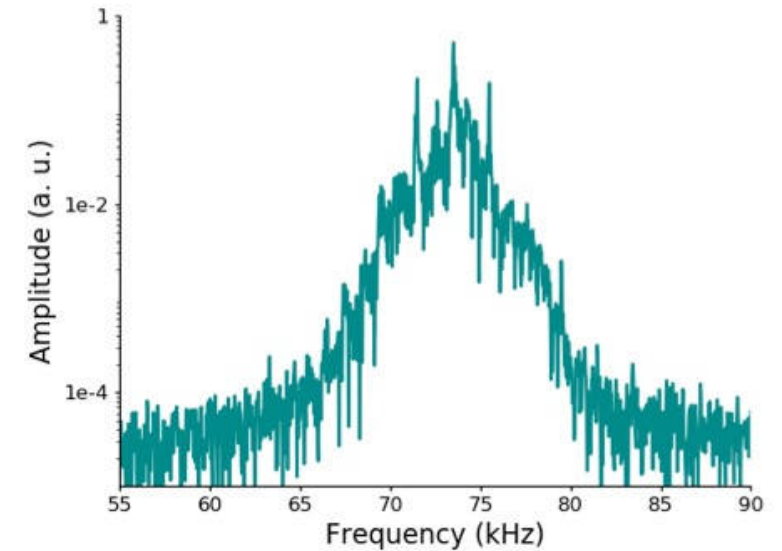
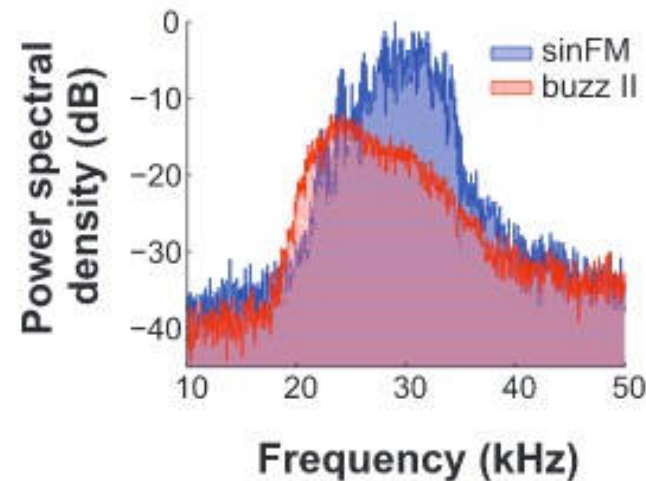
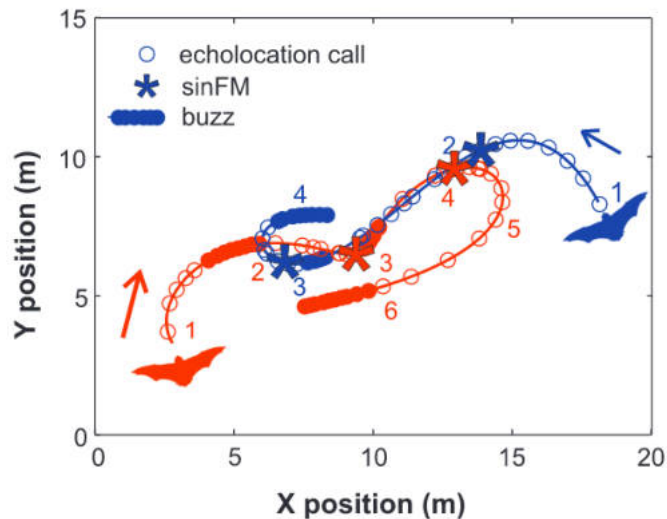
Corcoran *et al*, Science (2017)

## Bats jam bats for food competition

Corcoran *et al*, Science (2014)

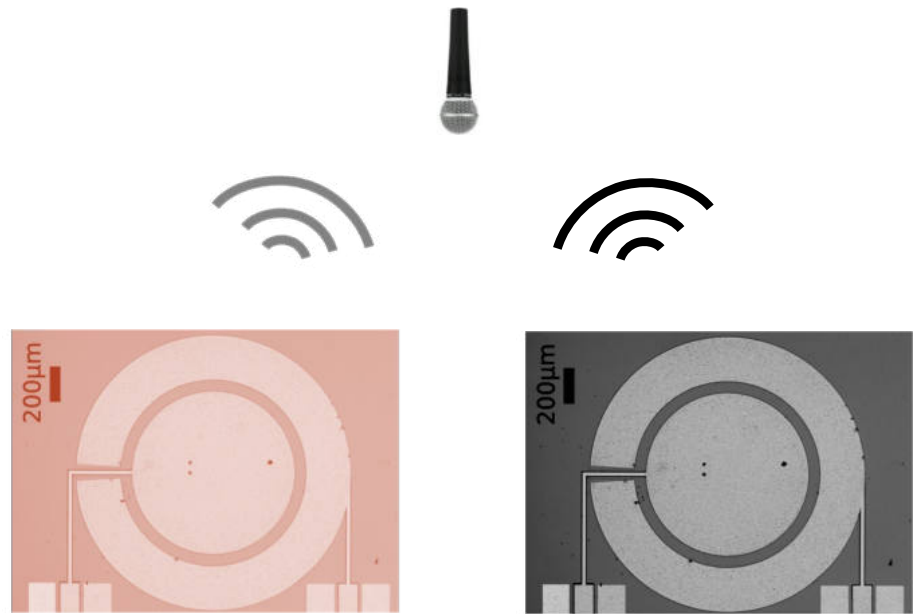


## Chaotic PMUT frequency spectrum



Defoort *et al*, JMM (2021)

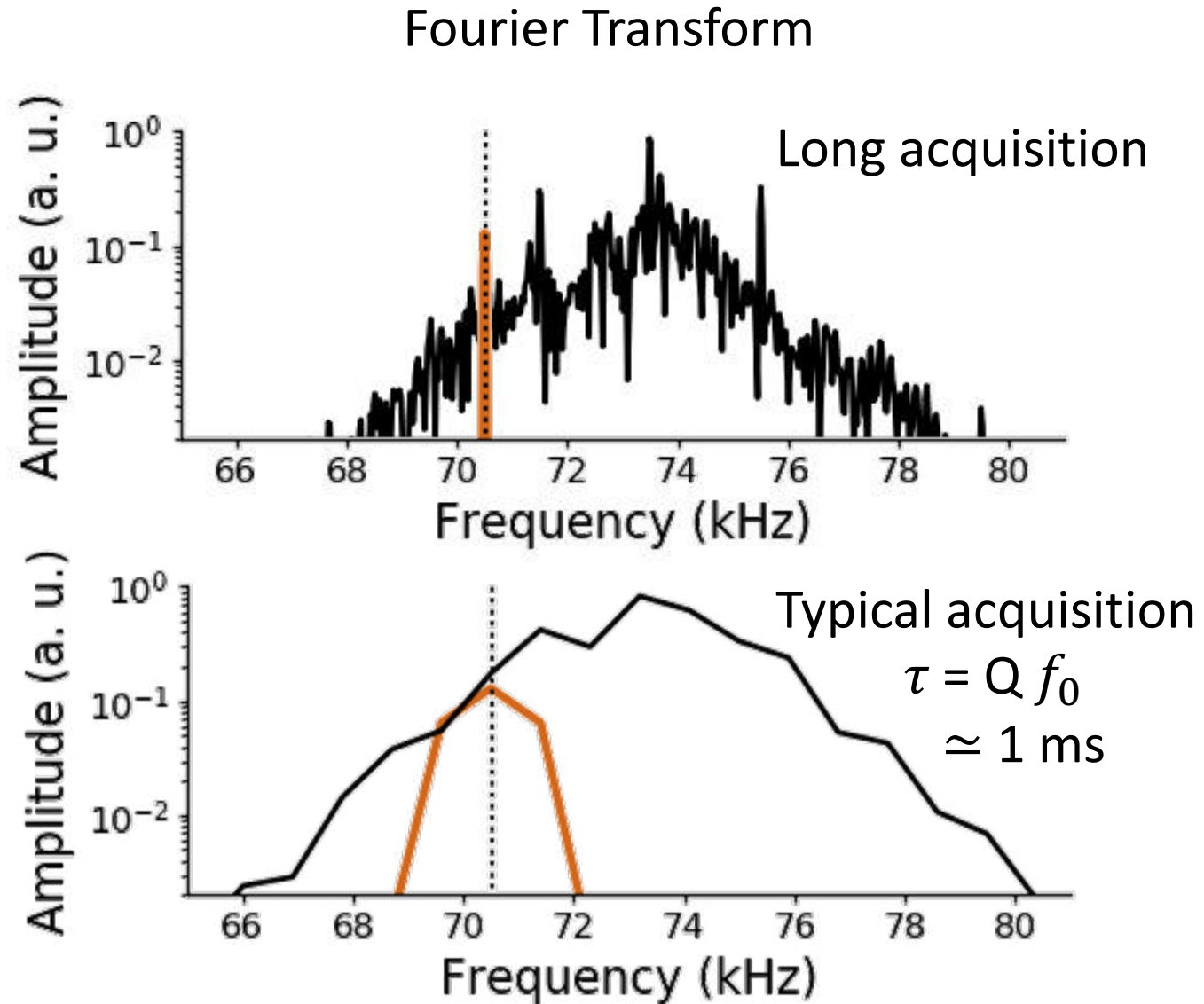
Using a chaotic PMUT to jam a standard PMUT



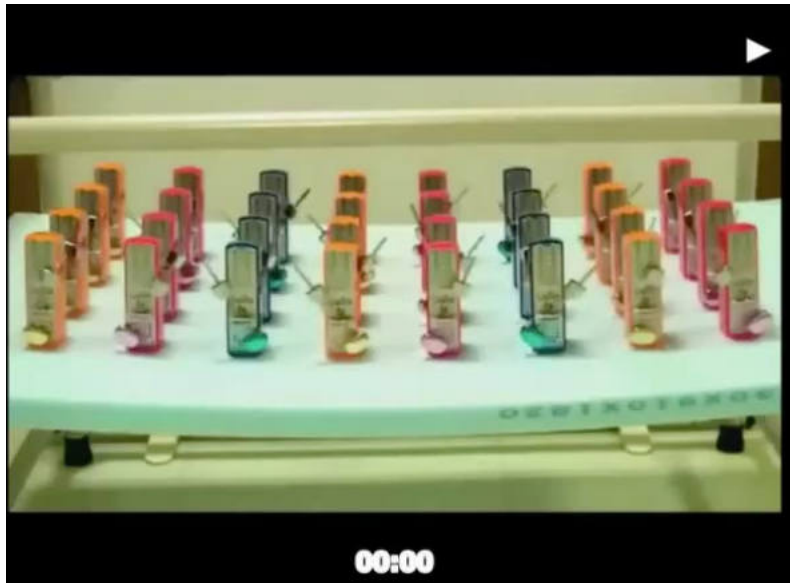
Emitter  
(linear PMUT)

Jammer  
(chaotic PMUT)

Acquisition time x8



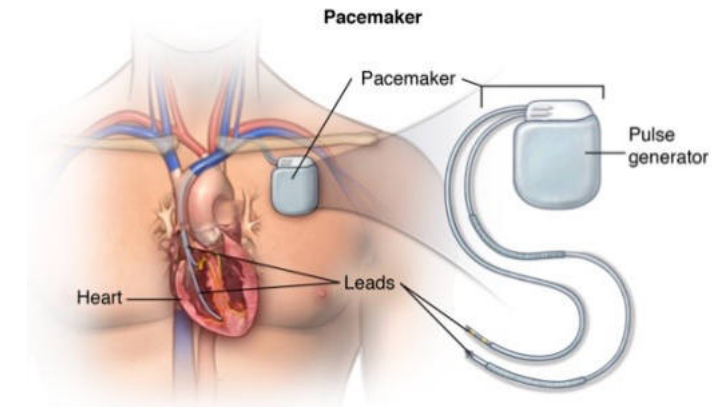
# Synchronization of chaotic MEMS



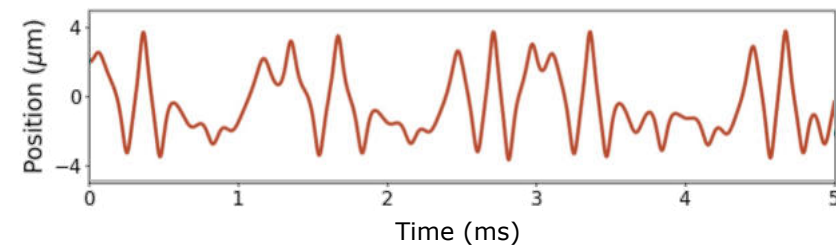
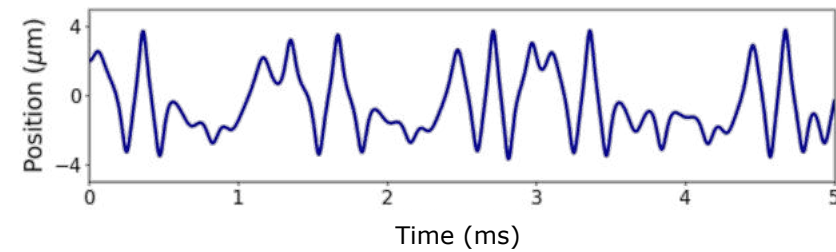
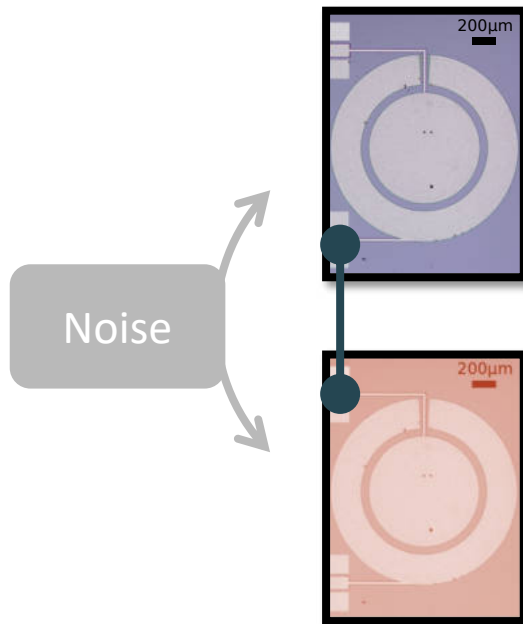
youtube.com

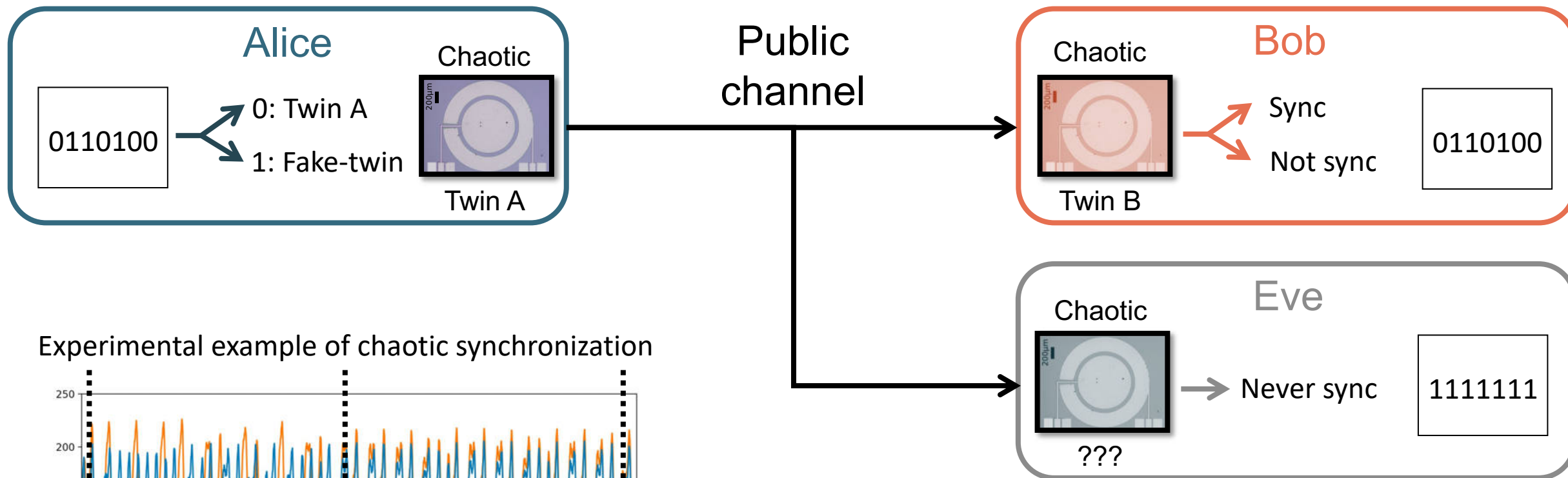


youtube.com

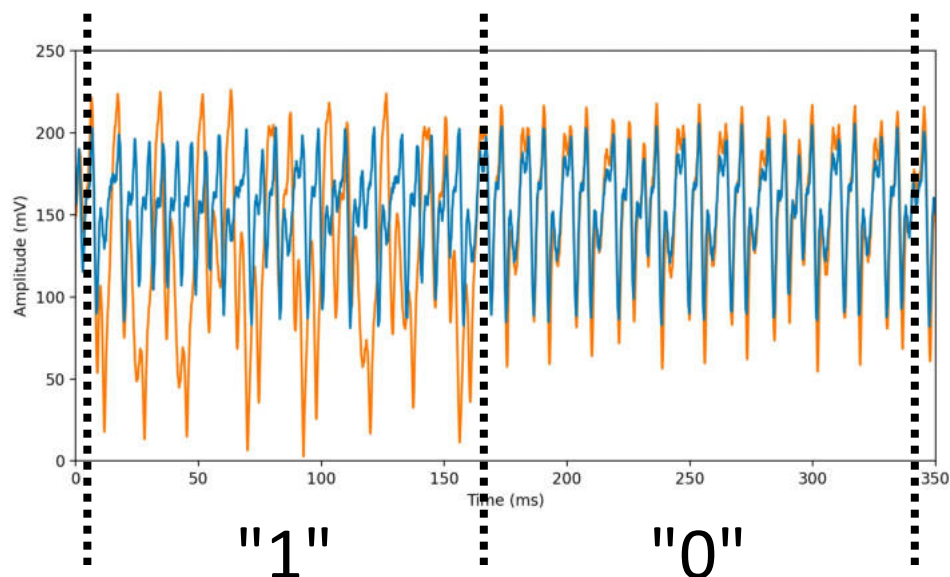


healthcare.utah.edu





Experimental example of chaotic synchronization



Chaotic cryptography => chaotic steganography

- Uses noise-like pattern to hide information
- Uses synchronization to decipher the "noise"
- Works only for very similar parameters (~ the key)

## Chaos in a non-linear non-buckled microresonator

- Based on Duffing regime
  - ➔ Reachable with any MEMS
- Model system
  - ➔ Figures of merit in quantitative agreement with simulations
- Applications
  - ➔ Sensors and actuators
  - ➔ Cryptography

